RUNNING HEAD: MODELLING SPATIAL IMMEDIATE SERIAL RECALL

Modelling spatial immediate serial recall performance in a macaque (Macaca mulatta)

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Abstract Botvinick et al (2009) examined the immediate 21 1 serial recall (ISR) capabilities of a rhesus macaque using 2 a spatial short-term memory task akin to that employed in 3 human memory studies. They found that the monkey's per-4 formance exhibited several hallmark effects of human ISR, 5 suggesting that computational mechanisms of human short-6 term serial order memory may therefore be appropriate 7 for understanding ISR in some nonhuman primate species. 8 Here I applied a computational model of short-term mem-9 ory that instantiates four core mechanisms of human ISR-10 competitive queuing, position marking, a primacy gradi-11 ent, and response suppression-to their monkey's data. The 12 model provided an excellent account of the monkey's ISR 13 performance and its capacity to do so was greatly dimin-14 ished when one or more of the mechanisms was eliminated 15 from the model, suggesting that all four mechanisms-16 rather than a restricted set of those mechanisms-is re-17 quired to explain the data. The results of the current simula-18 tion study suggest that common mechanisms may underpin 19 short-term serial order memory across species. 20

Keywords Serial order · Macaque · Short-term memory

The ability to encode, store, and recall arbitrary fixed 22 sequences of items, actions, and events is a fundamental hu-23 man cognitive skill. This kind of sequence learning has been 24 studied extensively in humans using the immediate serial 25 recall (ISR) task in which participants are given novel se-26 quences of verbal, visual, or spatial items that they must sub-27 sequently recall in the correct order. Considerable progress 28 has been made in understanding the cognitive components 29 underpinning this seemingly simple task thanks to the de-30 velopment of several computational models of short-term 31 memory that explain detailed aspects of the human ISR data 32 using explicit mechanisms for the representation of serial or-33 der (Botvinick and Plaut 2006; Brown et al 2000; Burgess 34 and Hitch 1999; Farrell and Lewandowsky 2002; Hartley 35 et al 2016; Henson 1998; Lewandowsky and Farrell 2008; 36 Page and Norris 1998). The analysis of recall error data have 37 played an instrumental role in constraining these models. 38 For example, error analyses have ruled out chaining mod-39 els in which order is stored through item-item associations 40 (Farrell et al 2013; Henson et al 1996), and conferred sup-41 port instead for positional models in which order is stored 42 through position-item associations (Conrad 1960; Henson 43 1999; Ryan 1969a,b). 44

The ability to learn arbitrary fixed sequences is not 45 unique to humans. Indeed, non-human primates (hereafter, 46 'primates') posses a remarkable capacity for mastering se-47 rial tasks. Monkeys can encode and reproduce the order 48 of arbitrary fixed sequences of visual images (Chen et al 49 1997; Orlov et al 2000; Terrace 2005) numerals (Inoue and 50 Matsuzawa 2007; Matsuzawa 1985; Kawai and Matsuzawa 51 2000), and spatial targets (Barone and Joseph 1989; Ker-52 madi and Joseph 1995). They can remember sequences con-53 taining as many as seven elements (Chen et al 1997) and 54 their performance on serial tasks has sometimes been shown 55





Fig. 1 Schematic of the spatial ISR task used by Botvinick et al (2009). The items were locations contained within a 3×3 visually presented grid. (A) At the start of a trial, the central location was illuminated and the animal was required to move a blue cursor from another location into the central location using a joystick, which caused the cursor to turn yellow. (B-D) Following the temporary disappearance of the cursor, a sequence of three or four locations—depending on the list-length; three in this example—was conveyed to the observing animal by highlighting an arbitrary sub-set of locations red, one location at a time. (E) Following a brief delay, the blue cursor re-appeared in the central location cueing the animal to reproduce the just observed sequence. (F) The animal used the joystick to move the blue cursor to the location corresponding to the first serial position—holding it in place briefly until the response was registered by the computer—before repeating this process for the locations corresponding to the second (G) and third (H) serial positions (and the location corresponding to the fourth serial position when the sequence length was four-items). Figure adapted from Botvinick et al (2009).

to exceed that of human participants (Inoue and Matsuzawa 80 57 2007). Like humans, monkeys are able to collectively plan short sequences of items prior to enactment (Biro and Mat-58 suzawa 1999; Inoue and Matsuzawa 2007; Kawai and Mat-59 suzawa 2000; Scarf et al 2011), and they appear to represent 60 sequences by forming associations between items and posi-61 tions, rather than between successive items (Carpenter et al 62 1999; D'Amato and Colombo 1988; D'amato and Colombo 63 1989; Orlov et al 2000, 2002, 2006). 64

Notwithstanding these similarities, as noted by 65 Botvinick et al (2009), until recently comparisons of the 66 sequence processing capabilities of humans and primates 67 had been hampered by the fact that studies with the two 68 groups have employed different tasks. The primate studies 69 have predominantly employed a serial learning paradigm 70 (Terrace 2005) in which monkeys gradually acquire se-71 quences over multiple encoding and recall attempts using a 72 forward training procedure-e.g., to acquire the sequence 73 $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F \rightarrow G$, the subject is trained to 74 respond A initially, then $A \rightarrow B$, then $A \rightarrow B \rightarrow C$, and so 75 on and so forth until the entire sequence can be produced. 76 As such, these studies probe long-term memory for serial 77 78 order, rather than short-term memory for serial order-the competency indexed by the ISR task used with humans. 79

5Spatial ISR in primates

This gap in the literature was recently filled by two stud-81 ies that examined the sequence processing abilities of a 82 single rhesus macaque (Botvinick et al 2009) and two ba-83 boons (Fagot and De Lillo 2011) using an ISR task for se-84 quences of spatial locations similar to that used to inves-85 tigate serial spatial short-term memory in humans (Jones 86 et al 1995; Smyth and Scholey 1996). Although both stud-87 ies showed that the ISR performance of monkeys exhibits 88 attributes of human ISR-notably list length and serial posi-89 tion effects (see below)—the study of Botvinick et al (2009) 90 is especially noteworthy, since these authors evaluated their 91 monkey's performance with reference to several benchmark 92 characteristics of human ISR, which included a detailed 93 analysis of recall error data. 94

The spatial ISR task employed by Botvinick et al (2009) 95 is illustrated graphically in Fig 1. The to-be-remembered 96 items were spatial locations (square icons) contained within 97 a 3 \times 3 visually presented grid. On each ISR trial, a se-98 quence of either three or four locations was conveyed by 99 sequentially highlighting a random sub-set of the locations, 100 after which the animal's task was to reproduce the sequence 101 using a joystick controlled cursor. The monkey's perfor-102



Fig. 2 The monkey's results for four key behavioural measures: (A) accuracy and repetition error serial position curves, (B) transposition error gradient for four-item lists, (C) aggregate spatial error gradients, and (D) spatial error gradients for the second, third, and fourth output position in four-item lists.

ISR, which are described in the foregoing sub-sections. 104

List length effect 105

In humans, ISR performance for lists composed of verbal 106 items (Crannell and Parrish 1957; Maybery et al 2002) and 107 spatial items (Jones et al 1995; Smyth and Scholey 1996) 108 decreases as the length of the target sequence to-be-recalled 109 increases-a result dubbed the list length effect. 110

Fig 2A shows the accuracy serial position curves for 111 three- and four-item lists for the monkey's performance. 112 Consistent with the list length effect in human ISR, it can 113 be seen that recall accuracy was lower for four- than three-114 item lists. 115

Primacy and recency effects 116

A hallmark feature of human ISR is the presence of serial 117 position effects on performance. Recall accuracy decreases 118 119 sharply from the first position onwards (viz. the primacy ef*fect*), with an upturn in performance for the final item (viz. 120

mance on this task exhibited several hallmarks of human¹²¹ to the recency effect), yielding an asymmetrically bowed serial position curve. Primacy and recency effects are a character-122 istic of both verbal ISR (Baddeley 1968; Henson et al 1996) 123 and spatial ISR (Jones et al 1995; Smyth and Scholey 1996) 124 performance in humans. 125

> Consistent with the human ISR data, it can be seen from 126 Fig 2A that the monkey exhibited a pronounced primacy ef-127 fect. However, at variance with those data it did not exhibit a 128 positive recency effect. Indeed, the monkey actually showed 129 a negative recency effect, with the accuracy of recall of the 130 final item on three- and four-item lists being lower than for 131 the penultimate item. 132

Transposition error gradients

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A large proportion of errors in human ISR are order er-134 rors involving the recall of items in the wrong serial posi-135 tions. These transposition errors exhibit a tendency to clus-136 ter around their correct serial positions-an empirical regu-137 larity known as the locality constraint (Henson 1996). Ac-138 cordingly, when the probability of a transposition is plot-139 ted as a function of transposition distance-viz. the ordinal 140 distance of the transposed item from its correct position-141 4

with the number of transpositions decreasing monotonically 143 with increasing transposition distance. The locality con-144 straint is a robust feature of both verbal ISR (Henson 1996; 145 Lewandowsky and Farrell 2008) and spatial ISR (Hurlstone 146 and Hitch 2015; Parmentier et al 2006; Smyth and Scholey 147 1996) performance in humans. 148

The transposition gradient for four-item lists associated 149 with the monkey's performance can be inspected in Fig 2B 150 from which it can be seen that transpositions obeyed the lo-151 cality constraint observed in humans. 152

Item similarity effect 153

Errors in human ISR sometimes involve confusions between 154 items that share similar characteristics. In verbal ISR, such 155 confusions are based on phonology as evidenced by the 156 phonological similarity effect (Baddeley 1966, 1968; Con-157 rad and Hull 1964)-lists of phonologically similar sound-158 ing items (e.g., B D G P T V) are recalled less accurately 159 than lists of phonologically dissimilar sounding items (e.g., 160 e.g., F K L R X Y). In spatial short-term memory, item con-161 fusion errors occur on the basis of the spatial proximity of 162 items (Hitch, 1974). Accordingly, when errors are plotted as 163 a function of spatial proximity to the correct item, the prob-164 ability of an error decreases monotonically with increasing 165 spatial distance-viz. a locality constraint over the spatial, 166 as opposed to temporal, distance between items (Hitch 1974; 167 Rerko et al 2014). In human spatial ISR, the magnitude of 168 such spatial errors is known to interact with serial position 169 (Farrand and Jones 1996; Farrand et al 2001). 170

Fig 2C plots the aggregate spatial error gradients for 171 three- and four-item lists for the monkey's performance (in 172 the figure, spatial proximity is represented using a Manhat-173 tan distance metric). Consistent with the locality constraint, 174 the gradients peak for one-apart spatial errors and decrease 175 monotonically with increasing spatial distance. The gradient 176 is also steeper for three- than four-item lists. Fig 2D plots 177 the individual spatial error gradients for the second, third, 178 and fourth output positions in four-item lists. It can be seen 179 that the distribution of spatial errors interacts with serial po-180 sition, with the error gradients becoming shallower at later 181 output positions. 182

In brief, consistent with the data from human spatial ISR 183 the monkey's performance was sensitive to the spatial simi-184 larity of items, and additionally this spatial similarity effect 185 interacted with serial position. 186

Repetition errors 187

Repetition errors-viz. the repeated report of an item pre-188 sented only once on the study list-are very rare in human 189

the resulting gradients peak for one-apart transpositions¹⁹⁰ ¹⁴verbal (Henson 1996; Vousden and Brown 1998) and spatial ISR (Hurlstone and Hitch 2015), accounting for around 191 1% (Hurlstone and Hitch 2015) to 5% (Henson 1996) of 192 all responses. The frequency of repetitions in human ISR 193 is known to increase with serial position (Henson 1996). 194

> The repetition error serial position curves for three- and 195 four-item lists for the monkey's performance are shown 196 alongside the accuracy serial curves in Fig 2A. Consistent 197 with the human ISR data, erroneous repetitions were rare 198 and their frequency increased across output positions. 199

Fill-in errors

Transposition errors in human ISR exhibit a particular pat-201 tern of sequential dependency. If an item *i* is recalled a po-202 sition ahead of its correct position (e.g., recalling Bxx fol-203 lowing the list ABC), item i - 1 is more likely to be recalled 204 at the next output position (e.g., BAx; known as a fill-in er-205 *ror*) than item i + 1 (e.g., BCx; known as an *infill error*). 206 Specifically, fill-in errors outweigh infill errors by a ratio of 207 approximately 2:1 in both verbal ISR (Farrell et al 2013; 208 Henson 1996; Page and Norris 1998; Surprenant et al 2005) 209 and spatial ISR (Guérard and Tremblay 2008). 210

This fill-in tendency is also a feature of the monkey's 211 ISR performance, which contained 46 fill-in errors and 10 infill errors, yielding a ratio of 4.6:1. 213

Protrusion errors

In human ISR, items that were not part of the study list 215 sometimes intrude into participant's recalls. These errors of-216 ten take the form of immediate intrusions, which occur when 217 a participant recalls an item from trial N - 1 on trial N de-218 spite the item not being present on the study list for that 219 trial. When these immediate intrusion errors occur they of-220 ten maintain their serial position from trial N - 1 (Conrad 221 1960; Henson 1996, 1999). These position-preserving in-222 trusions are known as protrusion errors (Henson 1996) and 223 their frequency of occurrence is greater than would be ex-224 pected by chance alone. 225

The monkey's ISR performance was also characterised 226 by protrusions. Out of 157 immediate intrusion errors on 227 four-item lists, 51 (32.5%) were protrusion errors that main-228 tained their position from the preceding trial-a rate greater 229 than would be expected by chance (25%; viz. 1/n—where n 230 is the list length). 231

Current study

As noted by Botvinick et al (2009), the correspondence be-233 tween the monkey's ISR performance and that of humans 234

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is striking and suggests that the mechanisms of serial order embodied in computational models of serial order in hu-236 man short-term memory might be extensible to some pri-237 mate species. The aim of the current study is to provide a 238 formal test of this possibility by applying a computational 239 model that implements the representational mechanisms that 240 have been found to underpin human ISR to their monkey's 241 data to establish if these mechanisms-or a restricted set of 242 these mechanisms-can reproduce his behavioural results. 243

The model is based on competitive queuing models 244 of serial behaviour (Glasspool 2005; Houghton 1990)-the 245 dominant class of models of human ISR (Brown et al 2000; 246 Burgess and Hitch 1999; Farrell and Lewandowsky 2002; 247 Henson 1998; Page and Norris 1998). In competitive queu-248 ing models, items are activated in parallel and the item with 249 the strongest activation level is selected for output. There is 250 already direct evidence that primates utilise the competitive 251 queuing mechanism based on electrophysiological record-252 ing data obtained whilst rhesus monkeys performed a serial 253 imitation task (Averbeck et al 2002, 2003a,b). In the com-254 petitive queuing model examined here, serial order is rep-255 resented by forming associations between items and a rep-256 resentation of the their ordinal sequence position (viz. po-257 sition marking), by encoding each item with progressively 258 less strength (viz. a primacy gradient), and by suppressing 259 items in memory once they have been recalled (viz. response 260 suppression). There is considerable evidence that these four 261 mechanisms are implicated in the representation of serial or-262 der in short-term memory in humans (Hurlstone et al 2014; 263 Lewandowsky and Farrell 2008). 264

A generic competitive queuing model of spatial ISR

266 Model architecture

Fig 3 shows a schematic of the architecture of the compet-267 itive queuing model, which comprises three distinct layers 268 of units-a context layer, an activation layer, and a selection 269 layer. The context layer maintains a distributed representa-270 tion of the current position in the list, whereas the activation 271 and selection layers implement a localist coding scheme, 272 whereby each unit corresponds to a different item (location) 273 in the 3×3 visually presented grid (Fig 1). The context 274 layer and activation layer are connected by a Hebbian weight 275 matrix within which short-term associations between items 276 and a representation of their position are stored. Each unit 277 in the activation layer has a connection to all other units in 278 the selection layer. The strength of these connections reflect 279 the similarity between each location with itself, and all other 280 locations in the visual grid. Accordingly, the connection is 281 strongest between each unit in the activation layer and its 282 corresponding unit in the selection layer, with the strength 283



Fig. 3 Schematic of the architecture of the competitive queuing model. Note that to avoid visual clutter only a subset of the units in each layer are shown; inhibitory connections from the selection layer to the activation layer are included only for two units; self-excitatory connections in the selection layer are omitted; and only adjacent-neighbour lateral inhibitory connections are illustrated in the selection layer. See main text for further details.

$$w_{ii}^{AS} = e^{-cd_{ij}},\tag{1}$$

where d_{ij} is the Manhattan distance between item *i* and ²⁸⁹ item *j*, which is given by: ²⁹⁰

$$d_{ij} = \sum_{l=1}^{k} |a_l - b_l|,$$
(2)

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In addition to the weighted connections from the ac-336 29Retrieval tivation layer, each unit in the selection layer has a self-298 excitatory connection and lateral inhibitory connections to 299 all other units in the selection layer. Each unit in the se-300 lection layer also has an inhibitory connection to its corre-301 sponding unit in the activation layer. 302

Encoding 303

The position of each item in a serial list is represented by a 304 16-element distributed context vector (with values between 305 -1 and +1) constructed so that the cosine similarity between 306 any pair of vectors decreases as an exponential function of 307 their absolute ordinal distance (Farrell 2006): 308

$$\cos\left(\mathbf{c}_{p},\mathbf{c}_{q}\right) = \boldsymbol{\phi}^{(|p-q|)},\tag{3}$$

where \mathbf{c}_p and \mathbf{c}_q are context vectors for positions p and 309 q, respectively, and ϕ is a parameter controlling the rate at 310 which similarity drops off with increasing ordinal distance. 311 The encoding of a list of items within the network is 312 carried out by imposing the context vector representing the 313 current list position over the context layer, activating the just 314 presented item in the activation layer-viz. setting its unit's 315 activation to 1, and the activation of all other units to 0-and 316 modifying the strength of the weight w_{ij}^{CA} connecting each 317 unit i in the activation layer and each unit j in the context 318 layer via Hebbian learning: 319

$$\Delta w_{ij}^{CA} = \eta_p \, a_i^A \, a_j^C, \tag{4}$$

where a_i^A is the activation of unit *i* in the activation layer, 320 a_i^C is the activation of unit j in the context layer, and η is 321 a learning rate parameter that governs the strength of the 322 context-item associations. Specifically, the strength of these 323 associations decreases exponentially across list positions ac-324 cording to a primacy gradient of encoding strength: 325

$$\eta_p = \theta^{p-1},\tag{5}$$

where θ is a parameter determining the steepness of the 326 primacy gradient over list positions. 327

The process just described encodes serial order through 328 position-item associations (viz. position marking). However 329 the primacy gradient in encoding strength means that the 330 representation of order contains an ordinal, as well as a 331 positional, component. Evidence that rhesus monkeys use 332 position-items associations has been obtained from posi-333 tional intrusion errors in a delayed sequence-recall task 334 (Orlov et al 2000, 2002, 2006). 335

At retrieval the context vector for the current recall position 337 is reinstated in the context layer and presented to the weight 338 matrix connecting it with the activation layer. The net input 339 to each item unit *i* in the activation layer net_i^A is given by: 340

$$net_i^A = \sum_j a_j^C w_{ij}^{CA} + \varepsilon(0, \delta^A), \tag{6}$$

where a_i^C and w_{ij}^{CA} are the same as before. This gener-341 ates an activation gradient over the item units such that the 342 unit corresponding to the item presented at the position be-343 ing cued will be activated strongest, with the activation of 344 units corresponding to neighbouring list-items falling off as 345 their ordinal distance from the cued item on the presented 346 list increases. The activations elicited by the reinstated con-347 text vector are augmented with zero-mean Gaussian noise ε 348 with standard deviation δ^A to simulate transposition errors. 349

A key feature of the competitive queuing approach is 350 that items are temporarily inhibited once they have been out-351 put by setting their activations to negative values. Accord-352 ingly, some mechanism is required to ensure that suppressed 353 items are briefly removed from the response competition. To 354 accomplish this, the activation of each item unit *i* in the ac-355 tivation layer a_i^A is subject to the following activation func-356 tion: 357

$$a_i^A(p) = \begin{cases} net_i^A(p) & \text{if } a_i^A(p-1) \ge 0, \\ net_i^A(p) + a_i^A(p-1) \exp(-\lambda) & \text{otherwise,} \end{cases}$$
(7)

To explain, if the activation of unit a_i^A at position *p*-1 is 358 equal to or greater than zero-viz. if that unit is not in a sup-359 pressed state—then its activation at position p is based on 360 the net input elicited by the reinstated context vector only, 361 otherwise its activation is the joint combination of the net 362 input elicited by the reinstated context vector and its cur-363 rent negative activation value. The activation values of sup-364 pressed items gradually recover from inhibition over recall 365 positions, with the extent of this release from inhibition be-366 ing governed by the parameter λ . 367

The most active item unit in the activation layer propa-368 gates its activation along its weighted connections to each 369 unit in the selection layer. The initial input to each unit *i* in 370 this layer a_i^S is given by: 371

$$a_i^S = a_{win}^A w_{iwin}^{AS} + \varepsilon(0, \delta^S), \tag{8}$$

where a_{win}^A is the activation of the winning item unit win in the activation layer and w_{iwin}^{AS} is the weight of its connec-372 373 tion with each unit i in the selection layer, which is gov-374 erned by equations 1 and 2. This results in the item unit in 375

activation layer being activated the strongest, with the ac-377 tivation of other item units decreasing as their spatial dis-378 tance from this item increases. The item unit activations in 379 the selection layer are supplemented with zero-mean Gaus-380 sian noise ε with standard deviation δ^S in order to simulate 381 spatial errors. The activations of item units in the selection 382 layer are iteratively updated over time according to the fol-383 lowing equation: 384

$$int_i^S(t) = a_i^S(t-1) \,\alpha + \beta \sum_{j \neq i} a_j^S(t-1) + \varepsilon(0, \delta^S), \tag{9}$$

where $int_i^S(t)$ is the internal activation—viz. the net in-385 put a unit receives from within the selection layer-of item 386 unit i at time t, $a_i^S(t-1)$ is its activation at the preceding 387 time step, $a_i^{S}(t-1)$ is the activation of each other item unit j 388 at the preceding time step, α is the strength of the recurrent 389 self-excitatory connections ($\alpha = 1.1$), β is the strength of the 390 lateral-inhibitory connections ($\beta = -0.1$), and ε and δ^{S} are as 391 before. Equation 9 implements a winner-takes-all "compet-392 itive filter" (Houghton 1990), which selects the most active 393 item for output. The initially most active item unit has the 394 advantage that it will send more activation to itself than any 395 other item unit, and will also receive the least lateral inhi-396 bition. As the unit activations are iteratively updated over 397 time this results in a gradual increase in the activation of the 398 strongest unit, and a gradual decrease in the activations of 399 the weaker units as they receive more lateral inhibition. 400

The competitive filter is applied for a fixed duration of 401 20 iterative cycles-sufficient time to identify an unambigu-402 ous response. The item with the strongest activation level 403 at the end of this period constitutes the network's response 404 for the current recall position. The recall of an item is fol-405 lowed by the suppression of its unit's activation in the ac-406 tivation layer by setting its activation level to a fixed sup-407 pressed value τ of -1. This implements the mechanism of 408 response suppression, which is a core ingredient in competi-409 tive queuing models. It was also assumed that the process of 410 generating an item for output adds noise to the representa-411 tions of yet to-be-recalled items-an assumption known as 412 output interference. Consistent with other network models 413 of serial recall (Brown et al 2000; Lewandowsky and Farrell 414 2008), this output-contingent interference was modelled by 415 adding zero-mean Gaussian noise with standard deviation 416 δ^{wCA} to each of the context-item weights linking the acti-417 vation and context layers following the output of each item 418 $(\delta^{wCA} = .04).$ 419

To model protrusion errors, the context-item weights were not refreshed (i.e., set to zero) at the start of each new simulation trial. Instead, the context-item associations established on each trial were stored on a common weight matrix. At the end of each simulation trial, the context-item weights

the selection layer corresponding to the winning item in the⁴²⁵ ³⁷were normalised so that recent weight changes were more activation layer being activated the strongest, with the acinfluential than earlier weight changes.

Modelling negative recency

One challenge in modelling the monkey's data is captur-428 ing the negative recency effect. This effect is difficult to 429 reproduce using the model just described because compet-430 itive queuing models are by design configured to generate 431 a recency (along with a primacy) effect. There are several 432 factors that promote recency in the current model. One fac-433 tor is "edge effects"-because the last item only has neigh-434 bouring competitors on one side of the list it will be re-435 called with a higher level of accuracy than items at medial 436 serial positions, which have neighbouring competitors on 437 both sides of the list. Another contributing factor is response 438 suppression-as recall progresses, the cohort of recall can-439 didates gradually winnows down due to the suppression of 440 items already emitted, which increases the likelihood that 441 the final item will be assigned to its correct position. 442

Modelling the negative recency effect is necessary not 443 just in terms of providing an explanation for its presence 444 in the monkey's data but because it is impossible to recre-445 ate the distributions of the various different errors without 446 modelling the sharp decline in recall accuracy toward the 447 end of the list. How then to explain this result? One expla-448 nation offered by Botvinick et al (2009) is that it might be 449 due to interference caused by irrelevant events-including 450 a tone and a juice reward-that were interspersed between 451 each recall episode. This interference is not dissimilar to the 452 output interference implemented in the current model and 453 provides an additional precedent for its incorporation. How-454 ever, output interference alone was found to be insufficient 455 to generate the sharp drop in recall over the final two serial 456 positions. Another possibility-and the explanation pursued 457 here-is that this effect reflects the action of a selective en-458 coding strategy adopted during the encoding of serial lists. 459 This account supposes that the monkey allocated most of his 460 attention to encoding the first and second item in each list, 461 with a subsequent sharp drop in the attention allocated to 462 encoding the third item (in three- and four-item lists), and a 463 further abrupt drop in the attention allocated to encoding the 464 fourth item (in four-item lists). 465

This selective encoding strategy was implemented through the following modification to equation 2 that generates the primacy gradient governing the encoding strength of the context-item associations across serial positions: 469

$$\eta_{p} = \begin{cases} \theta^{p-1} & \text{if } p \le 2, \\ \theta^{p+1} & \text{if } p = 3, \\ \theta^{p+3} & \text{if } p = 4, \end{cases}$$
(10)

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The encoding strength of the first two items in the list is 16 47 Model comparisons calculated in the same way as in equation 2. However, the 471 encoding strength of the third item (on three- and four-item 472 lists) is calculated as though this were the fifth item on a 473 longer sequence, whilst the encoding strength of the fourth 474 item (on four-item lists) is calculated as though this were the 475 eighth item on a longer sequence. As desired, this produces 476 a sharp drop in encoding strength from input position 2 to 477 3, and another sharp drop in encoding strength from input 478 position 3 to 4. 479

Model fitting procedure 480

The to-be-fitted data consisted of the following behavioural 481 measures (27 data points in total): (1) accuracy serial posi-482 tion curves (seven data points), (2) repetition serial position 483 curves (seven data points), (3) transposition gradient (three 484 data points), (4) aggregate spatial error gradients (eight data 485 points), (5) proportion of fill-in to infill errors (one data 486 point), and (6) proportion of immediate intrusion errors that 487 were protrusions (one data point). Data for both list-lengths 488 were used for behavioural measures 1, 2, and 4, whereas 489 only the data for four-item lists were used for the other be-490 havioural measures (consistent with the reporting of these 491 data by Botvinick et al 2009). 492

To fit the model, predictions were generated for the 493 above measures for a set of starting model parameter values 494 and the discrepancy between the data and model predictions 495 was evaluated using the Pearson chi-square statistic: 496

$$\chi^2 = N \sum_i \frac{p_i - \pi_i}{\pi_i},\tag{11}$$

where p_i is the observed proportion for data point *i*, π_i 497 is the corresponding proportion predicted by the model, and 498 N is the number of observations. Since the chi-square statis-499 tic was calculated using observed and predicted proportions, 500 rather than frequencies, the value of N was simply set to 100. 501 The parameters of the model were varied systematically us-502 ing the SIMPLEX function minimisation algorithm (Nelder 503 and Mead 1965) until a minimum value of the chi-square 504 statistic was obtained. Each parameter vector explored by 505 the minimisation algorithm involved 2500 simulation trials 506 of three- and four-item lists. 507

The parameters that were varied during the fitting were 508 the degree of similarity of the context vectors ϕ ; the steep-509 ness of the primacy gradient in encoding strength θ ; the 510 amount of decay from response suppression λ ; the sensi-511 tivity parameter controlling the degree of confusability of 512 items in the selection layer c; the amount of noise in the ac-513 tivation layer δ^A ; and the amount of noise in the selection 514 layer δ^{S} (six free parameters in total). 515

The general model described above instantiates several dif-517 ferent mechanisms. To ensure that the incorporation of each 518 of these mechanisms is warranted and that the model is not 519 over-specified, model comparisons were performed in which 520 the fit of the general model was compared with that of sev-521 eral restricted model variants in which one mechanism (or 522 several) in the general model were eliminated. Specifically, 523 the fit of the general model was compared with that of three 524 restricted model variants: (a) a model in which response sup-525 pression was eliminated (removing two parameters; viz. τ , 526 and λ), (b) a model in which the primacy gradient was elim-527 inated (removing one parameter; viz. θ), and (c) a model in 528 which the primacy gradient and response suppression was 529 eliminated (removing three parameters; viz. θ , τ , and λ). 530 These models were fit to the behavioural measures in exactly 531 the same way as described for the general model, except that 532 the parameters associated with the eliminated mechanisms 533 were rendered inactive. 534

In addition to evaluating the models in terms of their best 535 fitting chi-square statistics, the Bayesian information crite-536 rion (BIC, Schwarz, 1978) was calculated. The BIC is an 537 index that takes into consideration both a model's goodness 538 of fit and its number of model parameters. The BIC was cal-539 culated as: 540

$$\operatorname{BIC}_{i} = V_{i} \ln(n) + n \ln\left(\frac{\operatorname{RSS}_{i}}{n}\right), \qquad (12)$$

where V is the number of free model parameters, n is the 541 number of data points being fitted, RSS is the residual sum 542 of squares, and *i* indexes the model for which BIC is being 543 calculated. 544

To aid interpretation, the raw BIC scores were converted 545 into BIC weights (Burnham and Anderson 2002; Wagen-546 makers and Farrell 2004), which express the degree of sup-547 port for each model on a continuous measure of evidence. 548 The BIC weight for model *i* was calculated by: 549

$$wBIC_i = \frac{\exp(-0.5\Delta BIC_i)}{\sum_{k=1}^{K} \exp(-0.5\Delta BIC_k)},$$
(13)

where ΔBIC_i is the difference in BIC between model *i* 550 relative to the best model, and each ΔBIC_k is the difference 551 in BIC between a specific model k in the candidate set K and 552 the best model. 553

Simulation Results

The goodness-of-fit quantities for the general model and the 555 three restricted model variants can be scrutinised in Table 1. 556 It can be seen by inspection that the general model obtained 557

 Table 1 Goodness-of-fit quantities for the general model and the threese

 restricted model variants.

Model	V	χ^2	BIC	∆BIC	wBIC
general	7	23.05	-168.79	0	1
restrict ^{PG+PM}	5	104.91	-102.22	66.57	0
restrict ^{PM+RS}	6	120.69	-93.93	74.86	0
restrict ^{PM}	4	114.51	-99.28	69.51	0

Note: V = number of free model parameters; χ^2 = Pearson chi-square statistic; BIC = Bayesian information criterion; Δ BIC = difference in BIC with respect to the best fitting model; wBIC = BIC weight. The bold item indicates the best fitting model.

the smallest χ^2 value, followed by the restrict^{*PG*+*PM*} model, then the restrict^{*PM*} model, with the restrict^{*PM*+*RS*} model obtaining the largest χ^2 value.

Before scrutinising the BIC scores, note that an extra pa-561 rameter was added to the value of V (the number of free 562 model parameters) prior to the computation of the BIC for 563 the general model and the restrict PM+RS model—taking the 564 value of V for these models from six to seven and five to 565 six, respectively. This extra parameter reflects the degree of 566 response suppression (τ). Although this parameter was not 567 varied in the fitting (it is by definition a fixed parameter), the 568 models nevertheless need to be penalised for containing an 569 extra parameter that is not present in the other two models. 570

Turning now to the BIC scores, the scores shown in 571 Table 1 confirm that the advantage of the general model 572 over the restricted model variants stands after controlling for 573 model complexity, and additionally the BIC weights indicate 574 that the evidence in favour this model is decisive. The best 575 fitting parameters for the general model are given in Table 2. 576 As the model comparisons confirm that the general model is 577 the preferred model of the data, for brevity, in what follows 578 I will only present the simulation results for this model. 579

580 List length, primacy, and recency

The accuracy serial position curves predicted by the general 581 model are shown in Fig 4A. It is apparent from inspection 582 of this figure that the general model predicted a small list 583 length effect, an extensive primacy effect, and a negative re-584 cency effect consistent with the empirical data (Fig 2A). The 585 list-length effect arises in the model because the more items 586 in the list, the greater the probability there will be at least one 587 error. The primacy effect is attributable to the primacy gra-588 dient in the encoding strength of items, whilst the negative 589 recency effect is the result of the selective encoding strat-590 egy built into the primacy gradient, which causes an abrupt 591 drop in encoding strength toward the end of the list thereby 592 counteracting the mechanisms that promote recency. 593

Consistent with the empirical transposition gradient for 595 four-item lists (Fig 2B), the transposition gradient predicted 596 by the general model for the same list length shows a posi-597 tional locality constraint-the gradient peaks for one-apart 598 transpositions and then decreases monotonically with in-599 creasing transposition distance (Fig 4B). Thus, when an item 600 was recalled in the wrong position, it tended to be recalled 601 in a position close to its correct position. In the model, the 602 positional locality constraint arises due to the local self-603 similarity of the context signal-neighbouring states (viz. 604 55@djacent serial positions) of context are more similar to one 605 another than states that are separated in ordinal distance (viz. 606 non-adjacent serial positions). This means that when a con-607 text pattern is presented to the activation layer, items that 608 are close in ordinal distance to the target item will be acti-609 vated more strongly than items that are far from the target 610 item in ordinal distance. Accordingly, when the item unit 611 activations are augmented with noise, near-neighbour trans-612 positions will be more likely than distant-neighbour trans-613 positions. 614

Spatial error gradients

As well as predicting a locality constraint for transposi-616 tion errors, the general model predicted a locality constraint 617 for spatial errors. In accordance with the monkey's data 618 (Fig 2C), the aggregate spatial error gradients predicted by 619 the model peak for one-apart spatial errors, with the fre-620 quency of errors decreasing monotonically with increasing 621 spatial distance, and additionally, the aggregate spatial error 622 gradient is steeper for three- than for four-item lists (Fig 4C). 623 Furthermore, it can be seen from inspection of Fig 4D that 624 the general model captured the reduction in slope of the in-625 dividual spatial error gradients with increasing output posi-626 tion for four-item lists that is a feature of the monkey's ISR 627 performance (Fig 2D). In the model, the spatial locality con-628

Table 2 Fixed and free parameter values for the general model.

Parameter	Description	Value
Fixed parameters		
α	Recurrent self-excitation	1.1
β	Lateral inhibition	-0.1
τ	Level of response suppression	-1
δ^{wCA}	Degree of output interference	0.04
Free parameters		
φ	Similarity of context vectors	0.6755
θ	Steepness of primacy gradient	0.7827
λ	Decay from response suppression	0.1631
с	Item confusability in selection layer	0.0713
δ^A	Noise applied to activation layer	0.0480
δ^{S}	Noise applied to selection layer	0.0055





Fig. 4 Predictions of the general model for the four key behavioural measures: (A) accuracy and repetition error serial position curves, (B) transposition error gradient for four-item lists, (C) aggregate spatial error gradients, and (D) spatial error gradients for the second, third, and fourth output position in four-item lists.

straint is a consequence of the exponential relation between650 similarity and spatial distance embodied in the weights link-630 ing item units in the activation and selection layers (equa-631 tions 1 and 2). This means that when activation from a win-632 ning item in the activation layer propagates through to the 633 selection layer, items that are spatially near to the target item 634 will be activated more strongly than items that are spatially 635 far from the target item. Accordingly, when the item unit 636 activations are augmented with noise, near-neighbour spa-637 tial errors will be more likely than distant-neighbour spatial 638 errors. 639

640 Repetition errors

The repetition error serial position curves predicted by the 641 general model are shown in Fig 4A. Consistent with the em-642 pirical data (Fig 2A), repetitions were infrequent and their 643 probability increased with output position. The scarcity of 644 repetitions in the model is due to the operation of response 645 suppression-the suppression of a recalled item's activation 646 in the activation layer removes it briefly from the response 647 competition, rendering it unlikely the item will be reported 648 twice. The probability of repetitions increases with output 649

⁶²position due to the greater time available for a suppressed item to recover from inhibition.

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Protrusion errors

The general model predicted a protrusion rate of 31.24% 653 (289 protrusions out of 925 immediate intrusions), which 654 compares favourably with the rate of 32.5% (51 protrusions 655 out of 150 immediate intrusions) exhibited by the monkey. 656 Immediate intrusions arise in the model because the context-657 item associations formed on different trials are stored in a 658 common Hebbian weight matrix-the associations formed 659 on trial n will be superimposed on the associations estab-660 lished on all trials so far. Thus, when a context cue for a 661 given position is presented to the activation layer on trial *n*, 662 as well as activating the target item on trial n and neighbour-663 ing list competitors, the context cue will activate the target 664 item and neighbouring list competitors from trial n-1 (and 665 to a lesser degree items from earlier trials whose associa-666 tions are less strongly represented in the weight matrix due 667 to the weight normalisation that occurs at the end of each 668 trial, which gradually washes out the influence of these as-669 sociations over time). With the addition of random noise to 670

item activations, sometimes the discrepancy between the ac-715 67 plan and produce sequences (Averbeck et al 2002, 2003a,b). tivations of items from trial *n* and trial n - 1 will be bridged, 672 triggering an intrusion. However, because the context-item 673 association of the item on trial n-1 that occupied the posi-674 tion being cued will bear a stronger similarity to the current 675 context cue than the associations of items from different po-676 sitions on trial *n*-1, intrusions will most often be protrusions. 677

Fill-in errors 678

The general model produced a fill-in ratio of 3.88:1 (101 fill-679 in errors vs. 26 infill errors), which is slightly smaller than 680 the observed ratio of 4.6:1 for the monkey's data (46 fill-in 681 errors vs. 10 infill errors). The predominance of fill-in events 682 in the general model is attributable to the representation of 683 serial order by a primacy gradient and response suppression. 684 This means that when an item *i* is reported a position too 685 soon and then suppressed, item i - 1 will be a stronger recall 686 competitor at the next output position than item i + 1 because 687 the former item-by virtue of occurring earlier on the study 688 list-will have been encoded with greater strength on the 689 primacy gradient. 690

Discussion 691

Summary of findings 692

Using computational simulations, the current study sought 693 to establish whether the spatial ISR performance of a rhe-694 sus monkey could be explained in terms of the seriating 695 mechanisms embodied in computational models of human 696 ISR. The results suggest that four core mechanisms of hu-697 man ISR-viz. competitive queuing, position marking, a 698 primacy gradient, and response suppression-are also im-699 plicated in the representation and control of serial order in 700 this primate species. The model comparisons confirmed that 701 all four mechanisms are necessary to accurately reproduce 702 the monkey's performance. That is, the correspondence be-703 tween the data and simulation results was severely compro-704 mised when one or more of the seriating mechanisms was 705 eliminated from the general model. In what follows, I will 706 describe those aspects of the monkey's data that confer sup-707 port for the different seriating mechanisms, consider some 708 limitations of the current modelling exercise, and identify 709 directions for future work. 710

Evidence for the four mechanisms 711

At the outset, it was noted that strikingly direct evidence has 712 713 been obtained from electrophysiological recording data that rhesus monkeys use the competitive queuing mechanism to 714

The results of the current simulation study provide converg-716 ing evidence for this proposition by showing that a model 717 based on competitive queuing principles can reproduce the 718 key behavioural features of a rhesus monkey's spatial ISR 719 performance. To my knowledge, this is the first computa-720 tional application of the competitive queuing mechanism to 721 serial order behaviour in a primate. 722

It is the model's capacity to reproduce the pattern of re-723 call errors seen in the monkey's spatial ISR performance 724 that is most emblematic of the operation of the competi-725 tive queuing mechanism. Like all competitive queuing mod-726 els, a defining feature of the current model is that items are 727 (re)activated in parallel at retrieval. There are two sources of 728 parallel response activation in the present model. The first 729 originates from the cueing of items in the activation layer by 730 the context vectors in the context layer. This results in the 731 target item being activated maximally, with neighbouring 732 items being activated based on their ordinal distance from 733 the target item in the input list. The second originates from 734 the retrieval of an item in the activation layer, which acti-735 vates items in the selection layer based on their similarity to 736 the retrieved item. Since the retrieved item will be most sim-737 ilar to itself, its unit will be activated maximally, whereas the 738 activation of other units will fall off with increasing spatial 739 distance from the retrieved item. The addition of moderate 740 random noise to item units in the activation and selection 741 layers is the basis by which the model generates transposi-742 tion and spatial errors, respectively. Since the activations of 743 items in both layers follow a gradient that is centred on the 744 target item, transposition and spatial errors are most likely to 745 involve items that are close in ordinal or spatial distance to 746 the target item. It is this parallel gradient-based response ac-747 tivation in the activation and selection layers-and the two-748 stage sequence production process-that enables the model 749 to reproduce the positional and spatial locality constraints 750 that are key features of the monkey's data. 751

The use of a two-stage sequence production process to 752 model spatial errors might seem unparsimonious. Why not 753 model spatial errors in the activation layer and do away with 754 the selection layer? Empirically, the observation of both a 755 positional and a spatial locality constraint suggests that the 756 effects of positional and spatial uncertainty arise indepen-757 dently, rather than additively. Indeed, an attempt to model 758 the data within a single stage by superimposing an activa-759 tion gradient representing the spatial uncertainty of items 760 over the activation gradient representing the positional un-761 certainty of items in the activation layer was unsuccess-762 ful. Specifically, this single-stage model generated viola-763 tions of both the positional and spatial locality constraints-764 the transposition error and spatial error gradients both ex-765 hibited marked non-monotonicities, at variance with the em-766 pirical data. Note also that in modelling phonological sim-767 ilarity effects in human verbal STM, the current dominants¹⁹ view is that a two-stage sequence production process is required, with the detrimental effects of phonological similarity occurring downstream of an initial serial ordering stage (Burgess and Hitch 1999; Henson 1998; Page and Norris 1998).

Although all errors generated by the model depend upon 774 the parallel sequence dynamics of the competitive queu-775 ing mechanism, the occurrence of certain errors is a con-776 sequence of the specific way serial order is represented. 777 Protrusion errors are a consequence of the representation 778 of serial order via position marking. The fill-in effect is a 779 consequence of the representation of serial order by a pri-780 macy gradient coupled with response suppression. If the lat-781 ter two mechanisms are eliminated, then the resulting model 782 (restrict^{PM}) predicts the same frequency of fill-in and infill 783 events (this is because after item *i* has been recalled a posi-784 tion too soon, items i - 1 and i + 1 will be activated to an 785 equivalent degree by the position marker for the next output 786 position), at variance with the monkey's performance. The 787 primacy gradient is also necessary to explain the extensive 788 primacy effect and flattening of the spatial error gradients 789 over output positions. When this mechanism is eliminated 790 (restrict PM+RS and restrict PM), the primacy effect is greatly 791 abated and the spatial error gradients over output position 792 become superimposed on one other. The main source of 793 evidence for response suppression is the scarcity of repeti-794 tions exhibited by the model, and the increase in these errors 795 across output positions. The latter result arises due to the 796 gradual wearing off of response suppression over output po-797 sitions. When this mechanism is eliminated from the model 798 (restrict PG+PM and restrict PM), much higher levels of recall 799 accuracy are observed at the third and fourth output posi-800 tions than observed empirically. This is because to compen-801 sate for the omission of response suppression, higher lev-802 els of accuracy at these positions are required to prevent the 803 model from generating excessive levels of erroneous repeti-804 tions. 805

806 Potential limitations and future directions

Although the model provides an excellent account of the ob-807 served hallmark effects, there are some limitations of the 808 current modelling exercise. First, the data and modelling are 809 based on a single animal. The theoretical inferences drawn 810 here will therefore need to be verified by showing that the 811 animal's ISR performance is representative of other animals 812 of the same species. Of particular interest is whether the 813 absence of recency is a defining feature of the ISR perfor-814 mance of macaque monkeys in general. It is noteworthy that 815 Fagot and De Lillo (2011) also failed to observe recency in 816 817 their study of the ISR performance of two baboons, tentatively suggesting that recency in ISR is a uniquely human 818

76attribute. However, in their study recency was merely absent, whereas in Botvinick et al (2009) recency was present 820 but in a negative, rather than a positive, direction. Second, 821 the explanation of negative recency in terms of selective en-822 coding is speculative. As noted by Botvinick et al (2009) it 823 could have been the consequence of the relatively long dura-824 tion of recall (7.5 s on average for three-item lists and 10.9 825 s on average for four-item lists) providing the opportunity 826 for time-based decay or interference of memory represen-827 tations. In modelling the present data, I considered this as 828 well as several other competing explanations, however, in 829 practice the selective encoding account was the only mecha-830 nism by which I was able to reproduce negative recency and 831 the correct underlying distributions of recall errors. 832

Although the monkey's ISR performance is qualita-833 tively consistent with that of humans-negative recency 834 notwithstanding-the maximum number of items it can re-835 tain is evidently much smaller. The sharp drop in recall per-836 formance after the second serial position implies a memory 837 span of around two-items, an empirical estimate that harmo-838 nizes well with the results obtained in other serial memory 839 studies with primates (Barone and Joseph 1989; Funahashi 840 et al 1997; Ninokura et al 2003; Scarf et al 2011). Human 841 adults, by comparison, have a memory span in the region 842 of six-items or greater. One question for future work is how 843 to explain these different memory limits in the model out-844 lined here? In some competitive queuing models-known as 845 normalised competitive queuing models (Bullock 2004)-846 the recurrent excitation and lateral inhibition implemented 847 in the selection layer is also instantiated in the activation 848 layer but in a way that encourages the maintenance of an ac-849 tivation pattern, rather than a winner-takes-all competition. 850 The effect of this is to impose a neural bandwidth limit on 851 the activation layer's capacity to maintain the relative prior-852 ity of a set of parallel activated memory representations. It 853 is possible that the smaller capacity limit seen in primates 854 is the result of less available neural bandwidth with which 855 to support parallel activated representations, perhaps due to 856 weaker levels of self-excitation or stronger levels of lateral 857 inhibition. 858

Concluding remarks

The present computational simulation study provides pro-860 visional evidence that four mechanisms of human ISR-861 competitive queuing, position marking, a primacy gradient, 862 and response suppression-are implicated in the representa-863 tion and generation of serial order in rhesus monkeys. The 864 observation of these mechanisms in a species of old world 865 monkey implies that they are ancient features in the evolu-866 tion of primates rather than bespoke components of human 867 cognition. This in turn suggests that the same mechanisms 868

- Compliance with ethical standards 871
- Conflict of interest 872
- The author declares that he has no conflict of interest. 873
- Ethical approval 874
- This article does not contain any studies with human partic-875 ipants or animals performed by the author. 876

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